

# Design Optimal Fractional Order PID Controller Utilizing Particle Swarm Optimization Algorithm and Discretization Method

Abdelelah Kidher Mahmood, Bassam Fadel Mohammed

**Abstract**—In this paper particle swarm optimization algorithm has been applied to design fractional order PID (FOPID) controller which has five unknown parameters to be tuned and determined by minimizing a given integral of time weighted absolute error (ITAE) as a fitness function. The FOPID controller is a special kind of PID controller whose derivative and integral order are fractional rather than integer which has five tuned parameters. The closed loop system for a plant cascaded with the fractional order PID ( $PI^\lambda D^\mu$ ) controller has been built utilizing a MATLAB/Simulink with application of intelligent optimization algorithm (PSO) as a sub program. The parameters of the  $PI^\lambda D^\mu$  controller found and injected to the controller structure. The main specification of this method is that the all five parameters of  $PI^\lambda D^\mu$  controller have been found directly without spreading the steps of computation. The results show performance of the closed loop system with FOPID controller is much better than integer order PID controller for the same system and with better robustness. The  $PI^\lambda D^\mu$  controller converted to z domain and programing to PIC microcontroller using new PIC Development Board.

**Index Terms**—Fractional calculus, fractional order controller, fractional order toolbox for MATLAB, MATLAB Simulink, PSO algorithm, continued fraction expansion (CFE), programing in C, PIC microcontroller.

## I. INTRODUCTION

The important requirements for a closed loop control system including the controller is to maintain the stability and robustness through the rejection of the disturbance and elimination of noise. The most popular controllers is the PID controllers which has parameters to be tuned to get a well specifications for the system both in time domain and frequency domain.

The PID controller that are significantly used in the industries and manufactures and in other domestic equipment's, which has three parameters to be tuned. Tuning PID controller is most important issue in industrial and process controllers due to its ability to tune the few parameters like proportional, integral and derivative manually or self-tune automatically. According to the Japanese electric measuring instrument manufacture's association in 1989, PID controller is used in more than 90% of the control loop. As an example for the application of PID controller in industry, slow industrial process can be pointed, low percentage overshoot and small settling time can be obtained by using this controller. In feedback control systems the controller function has ability to eliminate steady state offsets through derivative action.

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The derivative action in the control loop will improve the damping and therefore accelerating the transient response. Many theoretical and industrial studies have been done in PID controller setting rules like Ziegler and Nichol's in 1942 proposed a method to set the PID controller parameter Hägglund and Åström in 1955 and in 1999 changing in the technique have been introduced by them. By generalizing the derivative and integer orders, from the integer field to non-integer numbers, the fractional order PID control is obtained [1]. The performance of the PID controller can be improved by making the use of fractional order derivatives and integrals. This flexibility helps the design more robust system. The most important advantages of the  $PI^\lambda D^\mu$  controller is the better control of dynamical systems and less sensitive to changes of parameters of a control system [2]. Before using the fractional order controller in design an introduction to the fractional calculus is required. The first time, calculus generation to fractional, was proposed Leibniz and Hopital for the first time after words, the systematic studies in this field by many researchers such as Liouville 1832, Holmgren 1864 and Riemann 1953 were performed [1]. Due to widespread usage of PID controller in industries and product manufactures so researchers always motivated to look for a better and suitable design method or alternative controller [3]. For example, the fractional order algorithm for the control of dynamic systems has been introduced by utilization of CRONE (French abbreviation for Command Robusté d'Ordre Non Entier), over the PID controller, which has been demonstrated by Oustaloup [4]. Podlubny has proposed a generalization of the PID controller as  $PI^\lambda D^\mu$  controller which is known as fractional order PID controller, where  $\lambda$  is the non-integer order of integrator and  $\mu$  is the non-integer order of the differentiator term. He also demonstrated that the  $PI^\lambda D^\mu$  controller has better response than classical PID controller [5]. Frequency domain approaches of  $PI^\lambda D^\mu$  controller are studied in [6]. Also many valuable studies have been done for fractional order controllers and their implementations in [7]. Crucial importance of tuning of the controllers cannot be underestimated. Thus, many tuning techniques for obtaining the parameters of the controllers were introduced during last few decades. Tuning methods of  $PI^\lambda D^\mu$  controllers are recent research subject. Most of the researchers oriented to the classical optimization and intelligent methods [8]. Some tuning rules for robustness to plant uncertainty for  $PI^\lambda$  controller are given in [9]. However in order to achieve better results, there are still needs for new methods to obtain the parameters of  $PI^\lambda D^\mu$  controllers.

In this paper the Particle Swarm Optimization (PSO) algorithm has been used to tune the parameter of  $PI^\lambda D^\mu$  controller in order to get an optimum time domain specifications in which integral of time weighted absolute error (ITAE) has been minimized and the results

compared with conventional PID and with some other methods like the proposed method by (Vineet Shekher, Pankaj Rai and Om Prakash) [1], in which the parameters of  $PI^\lambda D^\mu$  controller has been obtained in three steps (Ziegler and Nichol's method to find proportional  $K_p$ , integral  $K_i$  parameters, Åström-Hägglund method to find derivative parameter  $K_d$  and the remained parameter  $\lambda$  and  $\mu$  found by optimization toolbox of the MATLAB "fsolve"). While in our optimization method, the five parameters found directly by utilizing PSO algorithm.

## II. FRACTIONAL CALCULUS

Fractional calculus is a generalization of integration and differentiation to non-integer order fundamental operator  ${}_a D_t^r$ , where  $a$  and  $t$  are the limits of the operation and  $r \in \mathbb{R}$ . The continuous Integra-differential operator is defined as:

$${}_a D_t^r = \begin{cases} \frac{d^r}{dt^r} & : r > 0, \\ 1 & : r = 0, \\ \int_a^t (d\tau)^{-r} & : r < 0. \end{cases} \quad (1)$$

The three equivalent definitions most frequently used for the general fractional differential are the Grünwald-Letnikov (GL) definition, the Riemann-Liouville (RL) and the Caputo definition. The GL definition is given by:

$${}_a D_t^r f(t) = \lim_{h \rightarrow 0} h^{-r} \sum_{j=0}^{\lfloor \frac{t-a}{h} \rfloor} (-1)^j \binom{r}{j} f(t-jh) \quad (2)$$

where  $[\cdot]$  means the integer part. The RL definition is given as:

$${}_a D_t^r f(t) = \frac{1}{\Gamma(n-r)} \frac{d^n}{dt^n} \quad (3)$$

for  $(n-1 < r < n)$  and where  $\Gamma(\cdot)$  is the Gamma function. The Caputo definition can be written as:

$${}_a D_t^r f(t) = \frac{1}{\Gamma(n-r)} \int_a^t \frac{f^{(n)}(\tau)}{(t-\tau)^{r-n+1}} d\tau \quad (4)$$

for  $(n-1 < r < n)$ . The initial conditions for the fractional order differential equations with the Caputo derivatives are in the same form as for the integer-order differential equations.

In the above definition,  $\Gamma(m)$  is the factorial function, defined for positive real  $m$ , by the following expression:

$$\Gamma(m) = \int_0^\infty e^{-u} u^{m-1} du \quad (5)$$

for which, when  $m$  is an integer, it holds that:

$$\Gamma(m+1) = m! \quad (6)$$

The definition of fractional derivative easily derives by taking an  $n$  order derivative ( $n$  suitable integer) of a  $m$  order integral ( $m$  suitable non integer) to obtain an  $n-m = q$  order one:

$$\begin{aligned} \frac{d^q f(t)}{dt^q} &= \frac{d^{n-m} f(t)}{dt^{n-m}} \\ &= \frac{1}{\Gamma(m) dt^n} \frac{d^n}{dt^n} \int_0^t (t-y)^{m-1} f(y) dy \end{aligned} \quad (7)$$

It must be noted that for  $q = 1$  ( $n = 2, m = 1$ ), (7) becomes the canonical first order derivative.

Laplace transform of non-integer order derivatives is necessary for an optimal study. Fortunately, not very big differences can be found with respect to the classical case, confirming the utility of this mathematical tool even for fractional systems. Inverse Laplace transformation is also useful for time domain representation of systems for which only the frequency response is known. The most general formula is the following:

$$L\left\{\frac{d^m f(t)}{dt^m}\right\} = s^m L\{f(t)\} - \sum_{k=0}^{n-1} s^k \left[ \frac{d^{m-1-k} f(t)}{dt^{m-1-k}} \right] \quad (8)$$

where  $n$  is an integer such that  $n-1 < m < n$ .

The above expression becomes very simple if all the derivatives are zero [10]:

$$L\left\{\frac{d^m f(t)}{dt^m}\right\} = s^m L\{f(t)\} \quad (9)$$

A fractional order system is that system described by the following fractional order differential equation:

$$\begin{aligned} a_n D^{an} f(x) + a_{n-1} D^{an-1} f(x) + \\ a_{n-2} D^{an-2} f(x) + \dots = b_n D^{\beta n} f(x) + \\ b_{n-1} D^{\beta n-1} f(x) + b_{n-2} D^{\beta n-2} f(x) + \dots \end{aligned} \quad (10)$$

where  $D^{an} = {}_0 D_t^{an}$ , is called the fractional derivative of order  $an$  with respect to variable  $t$  and with the starting point  $t = 0$ , [11].

## III. FRACTIONAL ORDER PID (FOPID) CONTROLLER

The integro-differential equation defining the control action of a fractional order PID controller is given by:

$$u(t) = K_p e(t) + K_i D^{-\lambda} e(t) + K_d D^\mu e(t) \quad (11)$$

where  $e(t)$  is the error signal of a tracking system,  $u(t)$  is the control signal, Applying Laplace transform to this equation with null initial conditions, the transfer function of the controller can be expressed by:

$$\begin{aligned} C_f(s) &= K_p + K_i s^{-\lambda} + K_d s^\mu \\ &= K \frac{\left(\frac{s}{w_f}\right)^{\lambda+\mu} + \frac{s \delta_f s^\lambda}{w_f} + 1}{s^\lambda} \end{aligned} \quad (12)$$

In a graphical way, the control possibilities using a fractional-order PID controller are shown in Fig. 1, extending the four control points of the classical PID to the range of control points of the quarter-plane defined by selecting the values of  $\lambda$  and  $\mu$  [12].

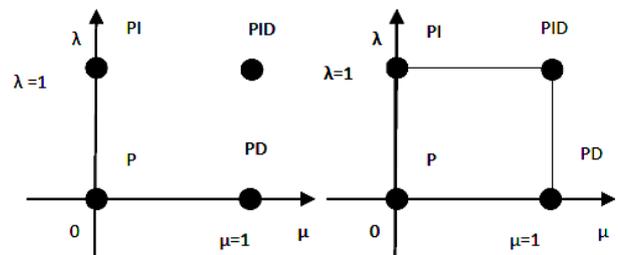


Fig 1. Fractional-order PID vs classical PID

## IV. PARTICLE SWARM OPTIMIZATION (PSO)

A special approach of swarm intelligence based on simplified simulations of animals' social behaviors, such as fish schooling and bird flocking, is the particle swarm optimization (PSO) algorithm. PSO is a self-adaptive search

optimization. The goal of particle swarm optimization is to solve the computationally hard Optimization problems, where it is a robust optimization technique based on the movement and intelligence of swarms and applied successfully to a wide variety of search and optimization problems. It was inspired from the swarms in nature such as swarms of birds, fish, etc. The PSO developed in 1995 by James Kennedy and Russ Eberhart. The algorithm adopted uses a set of particles flying over a search space to locate a global optimum, where a swarm of n particles communicate either directly or indirectly with one another using search directions, in each iteration of PSO, each particle updates its position based on three components, by determines its velocity using, previous velocity, best previous position, and the best previous position of its neighborhood. Fig. 2, illustrate the flow chart of PSO algorithm. The basic concept of PSO lies in accelerating each particle toward the best position found by it so far (*pbest*) and the global best position (*gbest*) obtained so far by any particle, with a random weighted acceleration at each time step, this is done by (13) and (14):

$$v_{t+1} = w * v_t + c_1 * rand(0,1) * (pbest - x_t) + c_2 * rand(0,1) * (gbest - x_t) \quad (13)$$

$$x_{t+1} = x_t + v_{t+1} \quad (14)$$

where: *gbest* = Global Best Position.  
*pbest* = Self Best Position.  
 $C_1$  and  $C_2$  = Acceleration Coefficients.  
 $w$  = Inertial Weight.

Once the particle computes the new  $x_t$  it then evaluates its new location. If fitness ( $x_t$ ) is better than fitness (*pbest*), then *pbest* =  $x_t$  and fitness (*pbest*) = fitness ( $x_t$ ), in the end of iteration the fitness (*gbest*) = the better fitness (*pbest*), and *gbest* = *pbest* [13].

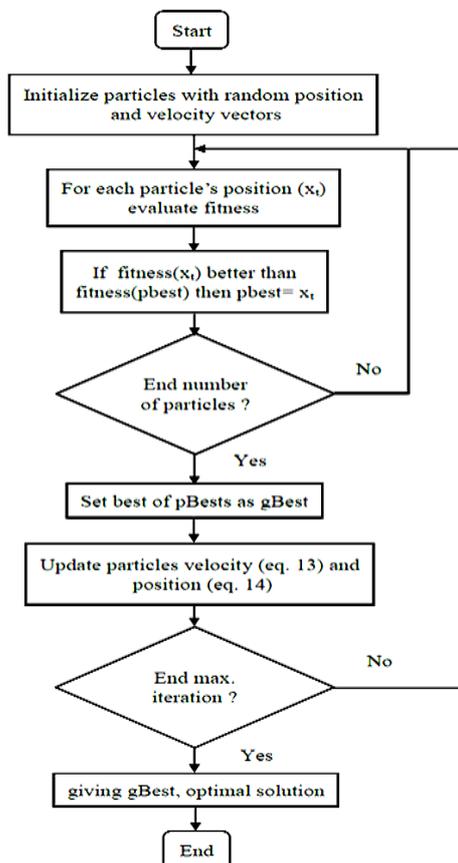


Fig 2. Flow chart of PSO algorithm

## V. DESIGN OF PI<sup>λ</sup>D<sup>μ</sup> CONTROLLER USING OPTIMAL PSO ALGORITHM

The closed loop system with negative unity feedback control system simulation shown in Fig. 3 with MATLAB, where the fractional order PID (FOPID) controller  $G_c(s)$  implemented by using fractional control toolbox [14], the integral of time weighted absolute error (ITAE) as objective function and the plant  $G(s)$  were implemented by MATLAB toolbox.

$$G_c(s) = K_p + \frac{K_i}{s^\lambda} + K_d s^\mu \quad (15)$$

$$G(s) = \frac{1}{(s^3 + 3s^2 + 2s)} \quad (16)$$

$$ITAE = \int_0^\infty t|e(t)|dt \quad (17)$$

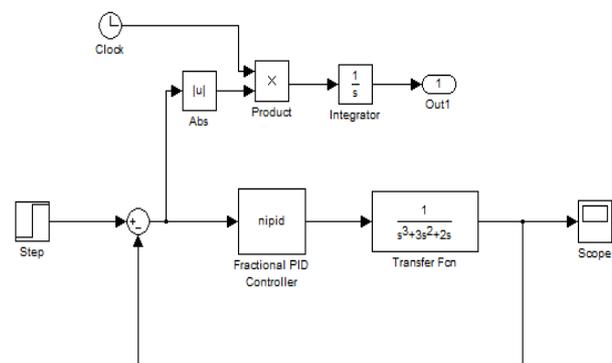


Fig 3. Negative unity feedback FOPID control system

The PSO algorithm method has been implemented as M file which interconnected to simulink model, where the FOPID controller parameters are computed and feed to the GUI of the controller. The optimization performed with this initial parameter, number of particles 30, number of dimensions 5, maximum iteration 50,  $C_1=1$ ,  $C_2=3$ , with the objective function ITAE. The initial values of five parameters  $K_p$ ,  $K_i$ ,  $K_d$ ,  $\lambda$ , and  $\mu$  of the fractional order PID controller will be generate in PSO program and submit in simulation diagram in Fig. 3, and running the simulation automatically then compute the objective function ITAE and go back with value of ITAE to PSO program to improve the value of  $K_p$ ,  $K_i$ ,  $K_d$ ,  $\lambda$ , and  $\mu$ , and go on. In the end of iteration the five parameters of the fractional order PID controller  $K_p$ ,  $K_i$ ,  $K_d$ ,  $\lambda$ , and  $\mu$  has been obtained directly according to the minimum value of objective function ITAE. The obtained results shown in the Table I.

Table I. Parameters of FOPID controller obtained by PSO algorithm

Tuning method and controller	Parameters				
	$K_p$	$K_i$	$K_d$	$\lambda$	$\mu$
PSO algorithm, (FOPID)	98.1959	0	70.9573	0	1.4497

Step response of the system in Fig. 3 for the FOPID controller tuned by PSO algorithm in Table I, illustrated in Fig. 4.

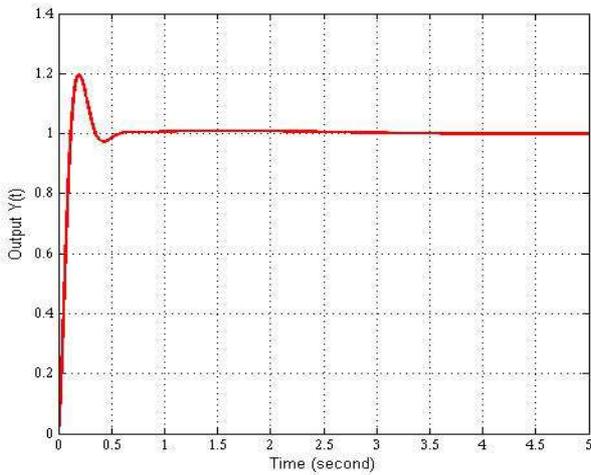


Fig 4.

Whereas the results that obtained in the proposed method by authors in [1] for  $\lambda$  and  $\mu$  and other parameters of the controller for different methods like Ziegler-Nichol's, Åström-Hägglund and the refsolver optimization method, shown in the Table II.

Table II. Parameters of PID & FOPID controllers obtained by different methods

Tuning method and controller	Parameters				
	$K_p$	$K_i$	$K_d$	$\lambda$	$\mu$
Ziegler-Nichol's, (PID)	3.6	1.63	1.98	1	1
Åström-Hägglund, (PID)	4.59	1.51	3.48	1	1
Proposed method in [1], (FOPID)	3.6	1.63	3.75	1.39	0.79

Step response of the system in Fig. 3, for each controller in Table II, illustrated in Fig.5.

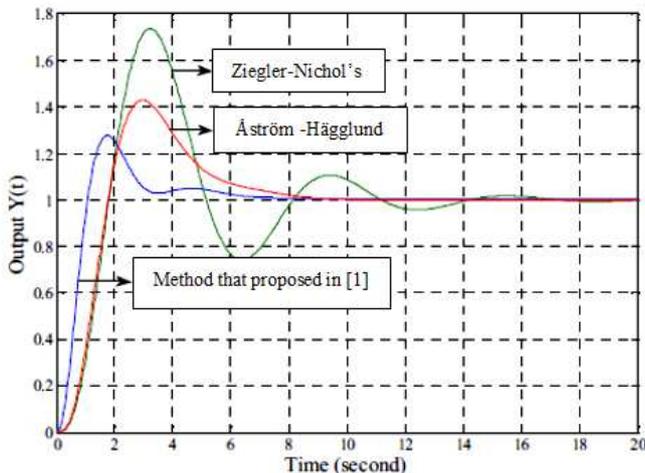


Fig 5. Step response of PID & FOPID control systems tuned by different methods

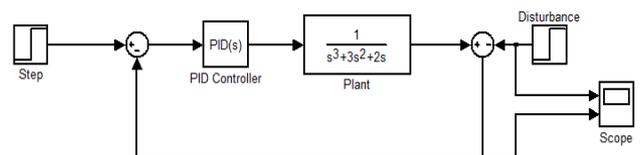
Step response of the system gives valuable information such as maximum overshoot (Mo.s %), rise time (  $T_r$  ), peak time (  $T_p$  ) and settling time (  $T_s$  ). It can be observed from the Table III, that the PSO algorithm method gives much better time domain performance with respect to the proposed methods in [1], specially for maximum overshoot(Mo.s%), rise time( $T_r$ ), peak time( $T_p$ ) and settling time( $T_s$ ).

Table III. Step response specification of PID & FOPID controllers

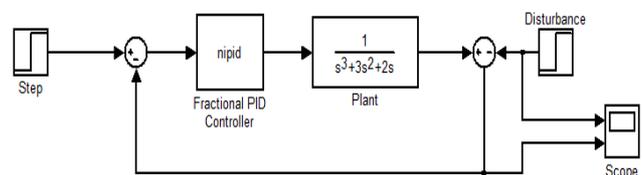
Tuning method and controller	Step response specification			
	Maximum overshoot (Mo.s %)	Peak time ( $T_p$ )	Rise time ( $T_r$ )	Settling time ( $T_s$ )
Ziegler-Nichol's,(PID)	73.5	1.67	3.25	12.5
Åström-Hägglund,(PID)	43	1.66	2.95	6.67
Proposed method in [1], (FOPID)	27.9	0.96	1.74	4.65
PSO algorithm, (FOPID)	19.7	0.195	0.084	0.476

### VI. ROBUSTNESS TEST OF THE SYSTEM

The main advantages of the fractional order controller are the robustness of the system whenever a disturbance occurred and in case of the uncertainty in the parameters. The system which has been designed tested by two type of disturbance one is when a load or perturbation was applied on the system. The second when selected parameters are deviated from its original value by 20%. Fig. 6 shown the simulation system for PID and FOPID controller with disturbance putting after the plant, because if the disturbance put between the controller and the plant the system never affect (i.e. the system is very robust).



(a)



(b)

Fig 6. (a) System for PID controller with disturbance, (b) System for FOPID controller with disturbance

Fig. 7 shown that the system for FOPID controller remains stable and very little effect on the time domain performance which means the sensitivity is very much low considering the deviated parameter from is original value.

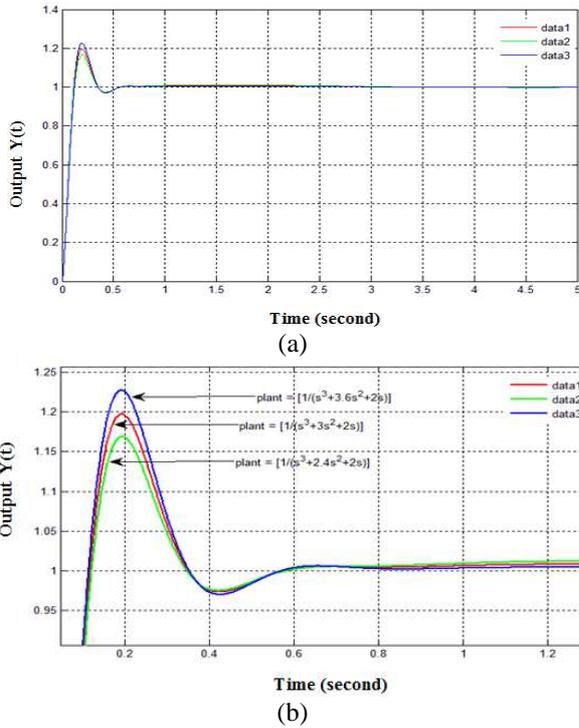


Fig 7. (a) Step response for system FOPID controller, (b) Focus (zoom) on (a)

Fig.8 shown the system sensitivity for FOPID controller is very low considering the disturbance effect compared with PID controller.

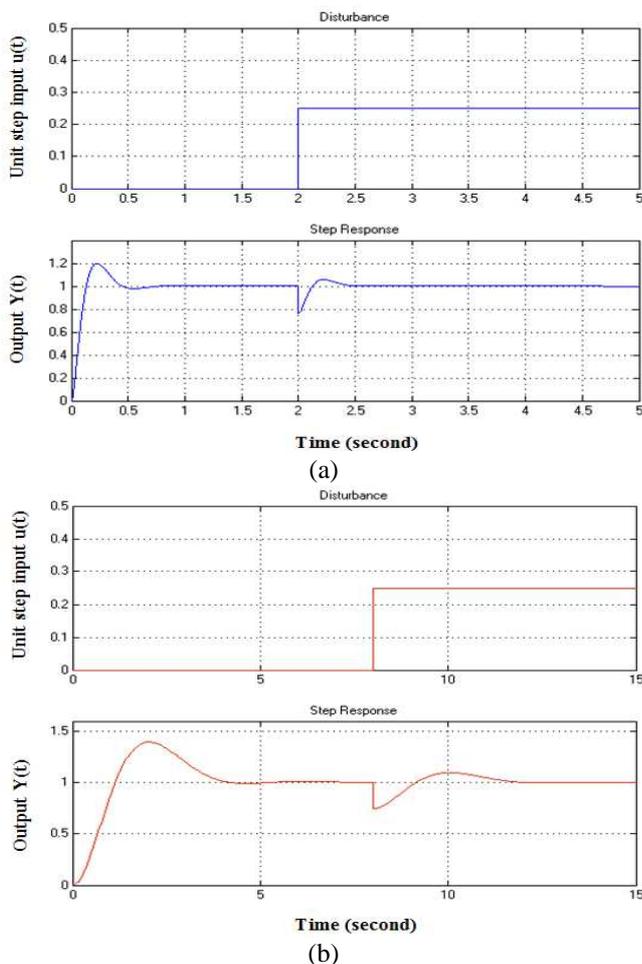


Fig 8. (a) Step response for system FOPID controller with disturbance, (b) Step response for system PID controller with disturbance

Table IV shown the time domain performance for the system FOPID controller with disturbance Fig. 8(a), is better than the system PID controller with disturbance Fig. 8(b).

Table IV. Step response specification of PID & FOPID controller with disturbance

System & tuning method of controller	Step response specification			
	Maximum overshoot (Mo.s %)	Peak time (Tp)	Rise time (Tr)	Settling time (Ts)
Åström-Hägglund (PID)	40	2	0.76	11.5
PSO algorithm, (FOPID)	19.7	0.23	0.091	2.38

### VII. DISCRETIZATION OF PI<sup>λ</sup>D<sup>μ</sup> CONTROLLER

In this paper used the direct discretization method include the continued fraction expansion (CFE) of Al-Alaoui operator, that is a new mixed scheme of Euler and Tustin operators. The resulting discrete transfer function, approximating fractional-order operators, can be expressed as:

$$D^{\pm r}(z) \approx \left(\frac{8}{7T}\right)^{\pm r} \text{CFE} \left\{ \left( \frac{1-z^{-1}}{1+\frac{z^{-1}}{7}} \right)^{\pm r} \right\}_{p,q}$$

$$= \left(\frac{8}{7T}\right)^{\pm r} \frac{P_p(z^{-1})}{Q_q(z^{-1})} \quad (18)$$

Where  $T$  is the sample period,  $P$  and  $Q$  are polynomials of degrees  $p$  and  $q$ , respectively, in the variable  $z^{-1}$  [15], [16], [17].

By the parameters in the Table I, the continuous transfer function of PI<sup>λ</sup>D<sup>μ</sup> controller can be expressed as:

$$G_c(s) = 98.1959 + 70.9573s^{1.4497} \quad (19)$$

The resulting transfer function of  $G_c(s)$  was obtained by using (18) and for  $T = 0.015$  second and  $p = q = n = 5$ , has the following form:

$$C_c(z) = \frac{4.744e07 - 1.407e08z^{-1} + 1.514e08z^{-2}}{1247 - 1639z^{-1} + 447.4z^{-2}} \frac{-6.995e07z^{-3} + 1.221e07z^{-4} - 3.571e05z^{-5}}{+ 65.91z^{-3} - 13.97z^{-4} - z^{-5}} \quad (20)$$

The transfer function (20) was rewritten to difference equation and was coded by PIC Micro C and then loaded to PIC18F45K22 memory by using the new PIC Development Board (EasyPIC v7 Development System) shown in Fig. 9 [18].

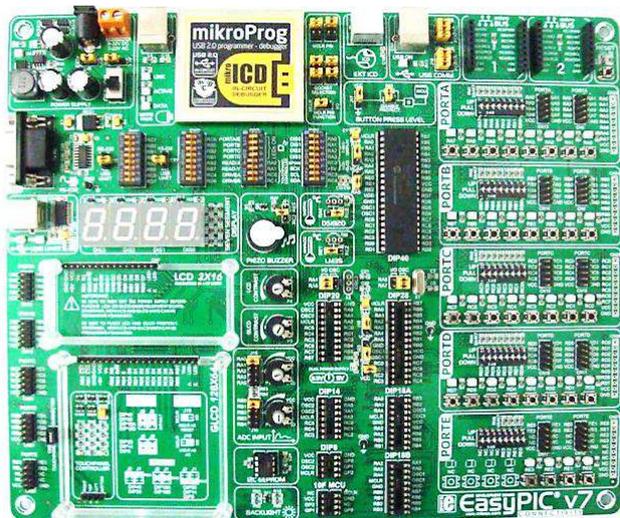


Fig 9.

The PIC Development Board for 250 Microchip PIC MCUs in DIP packaging. It features USB 2.0 programmer/debugger and over 17 essential modules necessary in development. PIC18F45K22 is the new default chip of EasyPIC™ v7! It has 16 MIPS operation, 64K bytes of on-line program memory, 3896 bytes of linear data memory, and support for a wide range of power supply from 1.8V to 5V. It's loaded with great modules: 36 General purpose I/O pins, 30 Analog Input pins (AD), Digital-To-Analog Converter (DAC), support for Capacitive Touch Sensing using Charge Time Measurement Unit (CTMU), three 8-bit timers and four 16-bit timers. It also has a pair of CCP, Comparators and MSSP modules (which can be either SPI or I<sup>2</sup>C). The discrete step response of the system in Fig. 3, illustrated in Fig. 10.

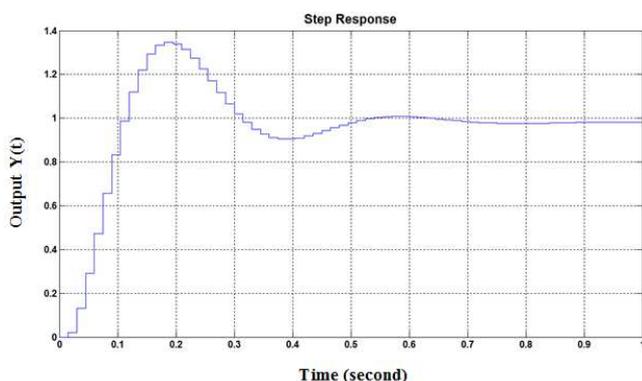


Fig 10. Discrete step response of negative unity feedback FOPID control system

### VIII. CONCLUSION

In this work the PSO algorithm has been utilized to find the optimal parameters of FOPID controller which minimize the ITAE. The major prosperities of our proposed method, the five parameters  $K_p$ ,  $K_i$ ,  $K_d$ ,  $\lambda$ , and  $\mu$  are found directly without spreading in steps and without need of finding the first three term of the controller. The system with FOPID controller exhibit good time domain response as compared with the integer order PID controller. Besides the system becomes more robust in which a good rejection of the disturbance and less sensitive to deviation in system parameters. The time

domain performance for the system exhibits a like response for both continuous and discrete time system.

### REFERENCES

- [1] V. Shekher, P. Rai, and O. Prakash, "Tuning and Analysis of Fractional Order PID Controller," International Journal of Electronic and Electrical Engineering, vol. 5, no. 1, 2012, pp.11-21.
- [2] D. Xue, C. Zhao, and Y. Q. Chen, "Fractional Order PID Control of a DC Motor with Elastic Shaft: A Case Study," Proc. of the 2006 American Control Conference, Minneapolis, Minnesota, USA, June 14-16, 2006, pp. 3182-3187.
- [3] K. J. Åström and T. Hägglund, PID controllers: Theory, Design and Tuning, 2nd Edition, Instrument society of America, 1995.
- [4] A. Oustaloup, F. Levron, B. Mathieu, and F. M. Nanot, "Frequency-Band Complex Non integer Differentiator: Characterization and Synthesis," IEEE Transactions on Circuits and Systems I: Fundamental Theory and Applications, vol. 47, no. 1, 2000, pp.25-39.
- [5] I. Podlubny, "Fractional-order systems and PID controllers," IEEE Transactions on Automatic Control, vol. 44, no. 1, 1999, pp.208-214.
- [6] B. M. Vingare, I. Podlubny, L. Dorcak, and V. Feliu, "On fractional PID controllers: A frequency domain approach," IFAC workshop on digital control. Past, present and future of PID control, 2000, pp.53-58.
- [7] Y. Q. Chen, and K. L. Moore, "Discretization schemes for fractional order differentiators and integrators," IEEE Transactions on Circuits and Systems I: Fundamental Theory and Applications, vol. 49, no. 3, 2002, pp.363-367.
- [8] C. A. Monje, B. M. Vingare, V. Feliu, and Y. Q. Chen, "Tuning and auto-tuning of fractional order controllers for industry applications," Control Engineering Practice, vol. 16, no. 7, 2008, pp.798-812.
- [9] C. A. Monje, A. J. Calderon, B. M. Vingare, Y. Q. Chen, and V. Feliu, "On Fractional PI Controllers: Some Tuning Rules for Robustness to Plant Uncertainties," Nonlinear Dynamics, vol. 38, 2004, pp.369-381.
- [10] R. Caponetto, G. Dongola, L. Fortuna, and I. Petráš, Fractional Order Systems: Modeling and Control Applications, Series A, vol. 72, Singapore: World Scientific Series on Nonlinear Science, 2010.
- [11] D. Baleanu, J. A. T. Machado, and A. C. J. Luo, Fractional Dynamics and Control, USA: Springer Science+Business Media, LLC, 2012.
- [12] C. A. Monje, Y. Q. Chen, B. M. Vinagre, D. Xue, and V. Feliu, Fractional-order Systems and Controls: Fundamentals and Applications, London: Springer-Verlag London Limited, 2010.
- [13] V. Gazi, and K. M. Passino, Swarm Stability and Optimization, German: Springer Science + Business Media, 2011.
- [14] D. Valério, Ninteger v. 2.3 Fractional control toolbox for MatLab, Lisboa: Instituto Superior Técnico da Universidade Técnica de Lisboa, 2005. Available:
- [15] M. A. Al-Alaoui, "Al-Alaoui Operator and  $\square$ -Approximation for Discretization of Analog Systems," SER.: ELEC. ENERG. vol. 19, no. 1, 2006, pp.143-146.
- [16] M. A. Al-Alaoui, "Novel digital integrator and differentiator," IEE Electronics Letters, vol. 29, no. 4, 1993, pp.376-378.
- [17] H. Sheng, Y. Q. Chen, and T. S. Qiu, Fractional Processes and Fractional-Order Signal Processing, London: Springer-Verlag London Limited, 2012.
- [18] PIC Development Board (EasyPIC v7 Development System). Available:<http://www.mikroe.com>.



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